## THE HISTORY OF THE SEVEN-DAY WEEK

BORIS ROSENFELD*

## 1. Numerical Weeks.

The seven-day week appeared in the Bible book Genesis in the account on the creation of the world in six days and was at first used by ancient Jews. The Hebrew name of the rest day Sabbath came from Babylonian name of the rest day sabbatum (Babylonians, like ancient Romans, used 7-8 day week determined by Lunar phases). The Hebrew names of days of the week are numerical Sunday -Yom rishon- "first day", Monday -Yom shani- "second day", Tuesday -Yom shlishi- "third day", Wednesday -Yom reve'i- "fourth day", Thursday -Yom khamshi- "fifth day", Friday -Yom shishi- "sixth day" and -Erev shabbat- "eve of Sabbath", Saturday -Yom ha-shabbat- "day of Sabbath". From Hebrew names came the Syriac names Hadbshabā, Trein-bshabā, Tlät$b s h a b \bar{a}, A r b a '-b s h a b \bar{a}, H a m e s h-b s h a b \bar{a},{ }^{\prime} R u b t \bar{a}$, Shabtā (first five names are connections of the numerals $1,2,3,4,5$ with the shortened name of Saturday and mean "first day after Saturday" and so on, the name of Friday means "preparation" since this day was the day of preparation to Saturday when any work was prohibited. From Hebrew names came also pre-Islamic Arabic names Yaum al-ahad, Yaum al-ithnayn, Yaum al-thalathā, Yaum al-arba‘a, Yaum al-khamis, Yaum al-'arūba, Yaum al-sabt. After the appearance of Islam Arabs replaced the name Yaum al-'arūba by Yaum al-jum'a- "day of meeting" (for prayers). Analogous to the Syriac names are the Persian names Yakshanba, Dūshanba, Seshanba, Chārshanba, Panishanba, Jum'a, Shanba (the Persian name of Friday is taken from Islamic Arabs).

Among the Greek names Kyriakē, Deutera, Tritē, Tetartē, Pemptē, Paraskeuē, Sabbato the name of Sunday means "day of the Lord", the names of 2th-5th days mean "second", "third", "fourth", and "fifth", the name of Friday mean "preparation" and is the translation of the Syriac name, the name of Saturday comes from Sabbath in some Byzantine documents Sunday is called Prōtē- "first" and Saturday is called Habdomē." "seventh." Among the Georgian names Kvira, Orshabat'i, Samshabat'i, Otkhshabat'i, Khutshabat'i, Paraskevi, Shabat'i and among Armenian names Kiraki, Erkushapt'i, Erek'shapt'i, Chorek'shapt'i, Hink'shapt'i, Urpat', 5th days are like in Syriac and Persian,

[^0]connections of the numerals $2,3,4,5$ with the name of Saturday, the names of Friday are versions of the Greek and Syriac names, the names of Saturday come from Sabbath.

The names of days of the week of many Muslim nations come from the Persian names: the Uzbeki and Tajiki names coincide with Persian names, the versions of these names are the Qazaq (Kazakh) names Jeksembi, Düysembi, Seysembi, Särsämbi, Beysembi, Juna, Sembi, the Qyrghyz (Kirgiz) names Jekshembi, Düysömbü, Sheyshembi, Shershembi, Beyshembi, Juma, Ishenbi, the Turkmen names Yekshenbe, Düshenbe, Sishenbe, Chärshenbe, Pershenbe, Anna, Shenbe, the Tatar names Yäkshämbe, Düshämbe, Sishämbe, Chärshämbe, Pän. jeshämbe, Jomgha, Shimbä, and the Bashqort (Bashkir) names Yäkshämbe, Düshämbe, Shishämbe, Sharshamby, Kesadhna, Yoma, Shmäbe (the Turkmen name of Friday and the Bashqort name of Thursday are old Turkic names). The versions of the Persian names are also some Azerbayjani and Turkish names: the Azerbayiani names are Bazar ("bazaar"), Bazar ertäsi ("day after Sunday"), Chärshänbä akshamy ("eve of Wednesday"), Chär. shänbä, Jümä akhshamy ("eve of Friday") Jümä, Shänbä, near to these names are Turkish names Pazar, Pazartesi, Sali (perhaps, the shortening of Sesembe), Çarşamba, Perşembe, Cuma, Cumartesi.

Among the Portuguese names the first and seventh Domingo ("day of the Lord") and Sabado (from Sabbath) are borrowed from Spanish and the other names Segunda feira, Terça feira, Quarta feira, Quinta feira, Sixta feira which are connections of the word feira-"bazaar" with the numerals "2nd", "3rd", ... " 6 th" are borrowed from Arabic.

The names of days of the week of many nations of Africa and Asia which obtained the 7-day week from Arab merchants come from the Arabic names: the versions of these names are the Hausa (Western Africa) names Lahàdi, Litiniǹ, Tàlātā, Lāràbā, Alhàmîs, Jumma'ā, Asabàr (the letter 1 in the beginning of some these names comes from Arabic article al-) the Malagasy (Madagascar) names Alahady, Alatsinainy, Talata, Alarobia, Alakamisy, Zoma, Asabothy (the letters al in the beginning of some these names also come from Arabic al-), and the Indonesian names hari Ahad, hari Senin, hari Selase, hari Rabu, hari Kamis, hari Jum'at, hari Sabtu. Among the Swahili (Eastern Africa) names Jumapili, Jumatatu, Jumanne, Jumatano, Alhamisi, Ijumaa, Jumamosi only the names of Thursday and Friday come from Arabic names, other names are formed analogously from the name of Friday and numerals mosi $=1$, mbili $=2$, tatu $=3$, nne $=4$, tano $=5$. Among Vietnamese names Chù nhàt, Thù' hai, Thù' ba, Thù'tu, Thù' năm, Thù' sau, Thù bay the first name means "day of Thù' hai, Thù' ba, Thù' tu, Thù' năm, Thù' sau, Thù' bay the
first name means "day of the Sun" or "day of the God", other names mean "2nd day", "3rd day", ... "7th day".

Besides numerical names of days of the week whose first day is Sunday (Biblical, Muslim and some Christian names) or Friday (Swahili names) there are also the numerical names whose first day is Monday-these names are used by Slavic and Baltic nations. The Russian names are Voskresen'ye (literally "resurrection" (of Christ) instead old Nedelya "'not working" that is the day when people do not work; now this word means in Russian "week'), Ponedel'nik ("day after Nedelya"), Vtornik (from, vtoroy"second"), Sreda (from, sredniz. "middle"), Chetverg (from chetvertyi"fourth"), Pyatnitsa (from pyaty̌̌", "fifth"), Subbota (from Sabbath). Analogous are the Ukrainian names Nedilya, Ponedilok, Vivtorok, Sereda, Chetver, P'yatnytsya, Subota, the Belorussian names Nyadzyela, Ponadzyelak, Awtorak, Sereda, Chats'ver, Pyatnitsa, Subota, the Polish names Niedziela, Poniedzialek. Wtorek, Sroda, Czwartek, Piatek, Sobota, the Czech names Nedelë, Pondēli, Utery', Streda, Cturtek, Pátek, Sobota, the Bulgarian names Nedelya, Ponedelnik, Vtornik, Sryada, Chetv"rt" $k$, Pet" $k, S$ "bota, the Serbian and Croatian names Nedelja, Ponedeljak, Utorak, Sreda, Ceturtak, Petak, Subota. The Lettonian names are Svētdiena, Pirmdiena, Otrdiena, Tresdiena, Ceturtdiena, Piektdiena, Sestdiena, the first of which means "day of Holiday", the other ones mean "1st day", "2nd day",... " 6 th day". The Lithuanian names are Sekmadienis, Pirmadienis, Antradienis, Trečiadienis, Keturiadienis, Penkiatdiena, S̈esstadienis, which mean "7th day", "1st day", "2nd day",... " 6 th day" respectively. The Estonian names are Pühapäev ("the holy day"), Esmaspäev ("1st day"), Teisipäev ("the other day"), Kolmapäev ("3rd day") or Kesknädal ("the middle of the week"), Neljapäev ("4rd day"), Reede (from Danish Fredag), Laupäev (from Danish Lördag). The Hungarian names are Vasárnap, Hétfö, Kedd, Szerda, Csütörtök, Pentek, Szom bat, the first from these names comes from Turkish Pazar (nap means "day"), the second and third names mean "head of the week" and "second", the last four names are versions of Slavic names.

These names are used also by some nations of the Northern Caucasus. The names of Ossetes, the descendants of Scythians, are Hu'ytsaubon ("day of the God"), Qu'yri-sär ("head of the week"), Dytztzäg ("second"), Artytztzäg ("third"), Tzyppäräm ("fourth"), Mayrämbon ("day of holiday"), Sabat (from Shabbath). The Chechen names are K'ira, Orshot (from Georgian Kvira and Orshabat'i), Shinara (from shi' $=2$ ), Khaara (from kho=3), Yieara (from di" = 4), P'eraska, Shot (from Georgian Paraskevi and Shabat'i). The names of Abaza are Mtshasha ("day of the Lord"), Khvasha ("5th day"), Sabsha (from Shabbath).

In Asia these names are used by Chinese, by Mongols, and by kindred to Mongols Buryats. The Chinese name Hsing ch'i jih of Sunday contains the word jih-"Sun", but the Chinese names Hsing ch'i $i$, Hsing ch'i erh, Hsing ch'i san, Hsing ch'i szu, Hsing ch'i wu, Hsing ch'i liu of other days contain the numerals $1,2, \ldots 6$. One of three kinds names of days of Mongols are Sayn ödör ("Holiday"), Negdekh ödör, Khoyordokh ödör, Guravdakh ödör, Dörövdökh ödör, Tavdakh ödör ("1st day", "2nd day", ..., "5th day"), Khagas sayn ödör ("eve of Sunday"). The Buryat names of days are Voskreseni (the version of the Russian Voskresen'ye), Garagan negen, Garagan khoyor, Gara-gan gurban, Garagan dürben, Garagan taban, Garagan zurgaan, Garagan doloon ("lst day", "2nd day"..., " 6 th day").

In Africa these names are used by some nations of Southern and Central Africa. Among the Zulu names Sonto, Msombulukwe, Wesibili, Wesithathu, Wesine, Wesihlanu, Mgibelo the first name is the version of the Dutch Zondag and the 3rd, 4th, 5th, and 6th names contain the numerals 2, 3, 4, 5 respectively. The Rwanda names Kucyumweru, Kuwanbera, Kuwakabiri, Kuwagatatu, Kuwakana, Kuwagatanu, Kuwagatandatu have the same meanings as mentioned above Mongol names.

The old Turkic names of days of the week are kept in the language of Karaims and Chuvashs whose languages are Turkic but who are not Muslims (Karaims are Judaists, Chuvashs are Christians). The names of days of Karaims living in the Crimea are: Yukh kun ("the day of the week") Yukh bash kun ("the first day of the week") Orta kun ("the middle day"), Khan kun ("the day of the king"), Kicheyne kun ("eve of Friday", of the Bashqort name), Eyne kun (of the Turkmen name), Shabbat kun ("the day of Sabbath'). The names of days of Karaims living in Lithuania are: Yekh kün, Yekh bash kün', Orta kün'; Khan kün,' Kichibaraski ('"eve of Friday"'), Baraski (from Greek Paraskeue and Anna kün,'Shabbat kün.' The Chuvash names are Vyrsarnikun, Tuntikun, Ytlarikun, Yunkun, Kesnernikun, Ernekun, Shamatkun, three last from these names are near to the Bashqort, Turkmen, and Karaim names of these days.

## 2. Planetary Weeks.

Besides numerical names of days of the week many nations of Europe and Asia have the names of days of the week which are connected with names of planets. These names appeared at first in ancient Rome and in India. The Roman names are Solis dies, Lunae dies, Martis dies, Mercurii dies, Jovis dies, Veneris dies, Saturni dies. In Christian Rome the names of Sunday and Saturday were replaced by Domini dies ("day of the Lord") and Sabbati dies respectively.

From the Christian Roman names come the Italian names Domenica, Lunedi, Martedi, Mercoledi, Giovedi, Venerdi, Sabato, the French names Dimanche, Lundi, Mardi, Mercredi, Jeudi, Vendredi, Samedi (earlier Sabedi) the Spanish names Domingo, Lunes, Martes, Miercoles, Jueves, Viernes, Sabado, the Rumanian and Moldovan names Duminică, Luni, Marti, Mercuri, Joi, Vineri, Sâmpată.

From the heathen Roman names come the English names Sunday, Monday, Tuesday, Wednesday, Thursday, Friday, Saturday, the German names Sonntag, Montag, Dienstag, Mitwoch, Donnerstag, Freitag, Sonnabend and Samstag, the Dutch names Zondag, Maandag, Dinsdag, Woensdag, Donderdag, Vrijdag, Zaterdag, the Swedish and Danish names Söndag, Mandag, Tisdag and Tirsdag, Onsdag, Torsdag, Fredag, Lördag, the Icelandic names Sunnudagr, Manadagr, Tyradagr, Odhinadagr, Thorsdagr, Frjadagr, Laugardagr. In the names of Germanic nations the names of Roman Gods Mars, Mercury, Jupiter (Jovis-Pater), and Venus are replaced by the names of corresponding Germanic gods Tir (or Tiw, Zio), the god of war, Wodan (or Odin, Wotan), later the chief god, but originally the god of the winds, Thor (or Donar), the god of thunder, and Freiya, the goddess of love. The German name of Wednesday means "the middle of the week", the first German name of Saturday means "eve of Sunday", the second one, as French Samedi came from Sabbath, the Scandinavian names of Saturday mean "the day of the bath". Among the Finnish names Sunnuntai, Maanantai, Tiistai, Keskiviikko, Torstai, Perjantai, Lauantai the first and last three names are veraions of Swedish names, the fourth one is the translation of the German name.

The names of the days of the week of Celtic nations also come from the Roman names: the Welsh names diw Sul, diw Llun, diw Mawrth, diw Merdhyr, diw lew, diw Gwener, diw Sadwrn come from the heathen Roman names. Among the Irish and Gaelio names Dé Domhnaigh, Dé Luain, Dé Mairt, Dé Ceadaoin, Déardaoin, Dé hAoine, Dé Sathairn the first name comes from the Christian Roman name, the 7th one comes from the heathen Roman name, the 2nd and 3rd names also come from the Roman names. Very near to Celtic names are Catalan names Diumenge, Dilluns, Dimarts, Dimeores, Dijous, Divendres, Dissabte which come from the Christian Roman names and the Albanian names Dielë, Hënë, Martë, Merkurë, Entjë, Prëmtë, Shtunë which come from the heathen Roman names (the first two Albanian names mean "the Sun" and "the Moon" respectively.

The Indian names, both classical Sanskrit and modern Hindi, are Aditya vara, Soma vara, Mangala vara, Budha vara, Brihaspati vara, Shukra vara, Shanayshohara vara, these names have the same meaning as the heathen Roman names. The names of days of the week of different nations of In-
dia are analogous to these names. The Marathi names are Ravi-war, Somawar, Mangal-war, Budh-war, Guru-war, Shukra-war, Shani-war (Rawi and Guru are other Sanskrit names of the Sun and Jupiter). The Urdu names are Itwar, Pīr (the Persian word meaning "old man"), Mangal, Budh, Juma'rat ('eve of Friday), Juma'a (from Arabic Jum'a), Haftah (the Persian word meaning "week").

The Indian names of days of the week were borrowed by all Asian nations professing Buddhism. The Thai (Siamese) names van Atit, van Chan (from Chandra, another Sanskrit name of the Moon), van Angkan, van Phut, van Prahat, van Suk, van Sau are versions of Indian names. Analogous are the Mongol names of the second kind Ad'yaa, Sum'yaa, Angarag, Bud, Burhaspad, Sugar, Sanchir. The Tibetan names of days of the week Nima, Dava, Migmar, L'agpa, P'urbu, Pasan, Panpa coinciding with the names of corresponding planets can be considered as translations of the Indian names. The Mongol names of the third kind Nyam, Davaa, Myagmar, Lhagva, Pürev, Baasan, Byamba are versions of the Tibetan names.

The Japanese names of days of the week Nichiyōbi, Getsuyōbi, Kayōbi, Suiyōbi, Mokuyōbi, Kin'yōbi, Doyōbi and the Korean names Ilyoil, Voryoil, Hwayoil, Suyoil, Moyoil, Kimyoil, Thoyoil also can be considered as translations of the Indian names also: the literal meanings of these names are "day of the Sun", "day of the Moon", "day of fire", "day of water", "day of wood", "days of metal (gold)", "day of earth (soil)", but the Chinese names of the planets Mars, Mercury, Jupiter, Venus, and Saturn are Huo hsing (the star of fire), Shui hsing (the star of water), Mu hsing (the star of wood), Chin hsing (the star of gold), T'u hsing (the star of soil) respectively (fire, water, wood, gold, and soil were five elements of classical Chinese science). Since the modern Chinese name of Sunday means "day of the Sun" and all other names of modern Chinese days of the week contain the character Hsing ""star", it is probably that the old Chinese names of days of the week had the same meanings as modern Japanese and Korean names and also were translations of the Indian names.

The ordering of the planets in the names of the days of the week and planets is explained as follows: each day of the week and each diurnal and nocturnal hour have the "celestial lord", the "lords" of days are "lords" of their first diurnal hours. The "lord" of the first diurnal hour of Sunday (and of Sunday itself) is the Sun, the "lord" of the second diurnal hour of Sunday is the following planet in the direction to the Earth in the Ptolemaic system, that is Venus, the "lord" of the third diurnal hour of Sunday is the following planet in the same direction, that is Mercury, the
"lord" of the fourth diurnal hour of Sunday is the Moon, the "lords" of the 5th-12th hours of Sunday are Saturn, Jupiter, Mars, the Sun, Venus, Mercury, the Moon, Saturn respectively. Therefore the "lord" of the 1st nocturnal hour of Monday is Jupiter, Jupiter is also the "lord" of 8th nocturnal hour of Monday, the "lords" of 9 th, 10 th, 11 th, and 12 th nocturnal hours of Monday are Mars, the Sun, Venus, and Mercury respectively, and the "lord", of the first diurnal hour of Monday (and of Monday itself) is the Moon. Analogously the "lords" of Tuesday, Wednesday, Thursday, Friday, and Saturday and Mars, Mercury, Jupiter, Venus, and Saturn respectively.

This system could appear only in the Hellenistic age when became wellknown the Biblical seven-day week, the division of day and night on 24 hours introduced by Egyptians and the Ptolemaic order of planets. Since this system in India was the same as in Rome, both systems had the common root. This common root probably was the Indo-Iranian cultus of Mithra very popular in the Roman empire.

The planetary names of days of the week appeared in Rome in I century A.D.: these names were used by the emperor Nero, whose letter to Cossus Lentulus begins as following: "Nerone Caesari Augusti Cosso Lentulo Cossi fil. VIII Idus febrariis dies solis, luna XIIIIX (sic) nun[dinis] Cumis V nun[dinis] Pomptis", ${ }^{2}$ this date is Sunday February 6 A.D. 60, 16th day of the Lunar month.

In Trajan baths on the Esquiline Hill in Rome was discovered the Roman calendar on which the months and the days of the months were marked by bone pegs inserted into the holes, the months were designated by zodiacal signs, the days of the month were defined by holes with numbers from I to XXX of the left and right sides of the calendar, the days of the week were defined by holes under the seven busts on the top of the calendar. Two busts were destroyed in the time of discovery of the calendar. These busts are personalizations of the days of the week: the first bust with rays symbolyses the Sun and Sunday, the second with two horns symbolyses the Moon and Monday, the third with the spear symbolyses Mars and Tuesday, the fourth with hare's ears symbolizes Mercury and Wednesday, the seventh with the star on his forhead symbolizes Saturn and Saturday, the busts symbolizing.Jupiter and Thursday and Venus and Friday are destroyed (see Fig. 1 borrowed from the paper of A. Cutler). ${ }^{3}$

[^1]On Fig. 2-6 are represented the gods Saturn, Mars, Mercury and the gods of the Sun and the Moon from a codex-calendar of A.D. 354 kept in the Vatican Library ${ }^{4}$ (Tables 8-12), under the image of each god is written the name of corresponding day "Saturni dies", "Martis dies" etc., on the left and right of these images the "lords" of the nocturnal and diurnal hours of the corresponding day of the week are indicated.

Probably in the same times these names appeared in India.
Let us note that the Latin names of days were still used in Europe in 19th century Martin Bartels (1769-1836), professor at the university in Kazan, Russia (where famous Nikolay Lobachevsky (1792-1856) was his student) wrote March 2, 1808 in a announcement. "Prof. math. purae Bartels in horis 7-9 antemeridianis dierum lunae et Jovis trigonometriam analyticam planam et sphaericam, et diei Saturni horis pomeridiani 4-6 applicationem ejus ad astronomiam sphaericam et geographiam mathematicam docebit" (Prodessor of the Pure mathematics Bartels will teach at 7-9 h. a.m. on Mondays and Thursdays Analytic trigonometry, both plane and spherical, and on Saturdays at 4-6 h. p.m. its application to Spherical astronomy and Mathematical geography). ${ }^{5}$

The correspondence between days of the week and planets was known also in Muslim countries and was described by Thābit ibn Qurra (836-901) in his Book on the subdivision of the days of the week according to sevenplanets written in his native Syriac (Aramaic) language. In this book Thābit ibn Qurra wrote: "The first day [Sunday] is devoted to the Sun whose name is Miyūs the second day [Monday] to the Moon whose name is $\operatorname{Sin} n$ the third day- to Mars whose name is Aris, the fourth day [Wednesday]- to Mercury whose name is Nabuq, the fifth day [Thursday] -to Jupiter whose name is $B \bar{a} l$, the sixth day (Friday)-to Venus whose name is Balth $\bar{\imath}$, the seventh day [Saturday]- to Saturn whose name is Qurunus. ${ }^{6}$ Here the god of the Sun, Mars, and Saturn are called by Greek names Helios, Ares, and Kronos, and the goddess of the Moon, Mercury, Jupiter and Venus are called by Babylonian names Sin, Nabo, Baal (Marduq), and Balthi (Ishtar). The book of Thābit ibn Qurra was translated into Arabic by his son Sinān ibn Thābit and this

[^2]correspondence is mentioned by al-Bīrūnī (973-1048) in his Astrology7, (No. 404) and by al-Najdī ( 15 th c.) in his Book on nautical uses. ${ }^{8}$

The names of days of the week of many former colonial nations are borrowed from languages of colonizers. We met the names of Sunday of Buryats and Zulu taken from Russian and Dutch. Besides the names of days in Hausa mentioned above there are the Hausa names Dimāsh $\bar{\imath}$ and Sàmdì of Sunday and Saturday taken from French. The names of days of Saha (Yakuts) living in Siberia Baskyhy'annya, Benidiennyik, Optuorunnyuk, Serede, Cheppier, Beetinse, Subuota are versions of Russian names. The names of days of Tagalogs living on Philippine Islands Linggo, Lunes, Martes, Miyerkoles, Huwebes, Biyernes, Sábado are versions of Spanish names.

The information about the names of the days of the week of the many nations discussed here has been derived from the book of F.K. Ginzel ${ }^{9}$ and from our previous paper (some mistakes which are in [10] are corrected here). ${ }^{10}$

The derivative history of these names clearly shows the cultural connections between different and sometimes very distant peoples.

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Fig. 1 - The Roman calendar from Trajan baths.


Fig. 2 - The planet Saturn, Romanus 1 ms., Barb. lat. 2154, fol. 8. Biblioteca Vaticana, Rome.


Fig. 3 - The planet Mars, Romanus 1 ms., Barb. lat. 2154, fol. 9. Biblioteca Vaticana, Rome.


Fig. 4 - The planet Mercury, Romanus 1 ms., Barb. lat. 2154, fol. 10. Biblioteca Vaticana, Rome.


Fig. 5 - The planet Sol. Romanus 1 ms., Barb. lat. 2154, fol. 11. Biblioteca Vaticana, Rome.


Fig. 6 - The planet Luna Romanus 1 ms., Barb. lat. 2154, fol. 12. Biblioteca Vaticana, Rome.


[^0]:    * Prof. Dr., Department of Mathematics, Pennsylvania State University.
    ${ }^{1}$ V. Grumel, La Chronologie, Paris, Presses des Universités, 1958, p. 166.

[^1]:    ${ }^{2}$ P. Brind'amour, Le calendrier romain, Ottawa, University Press, 1983, p. 268.
    ${ }^{3}$ A. Cutler, "Stalking the Beast Art History as Asymptotic Exercisc", Word and Image, vol. 7, 1991, No. 3, pp. 223-238.

[^2]:    ${ }^{4}$ M.R. Salzman, On Roman Time, the Codex-calendar of 354 and the Rythms of Urban Life in Late Antiquity, Berkeley, University Press, 1990.
    ${ }^{5}$ A.V. Vasil'yev, Nikolay Ivanovich Lobacheusky, Moscow, Nauka, 1992 (Russian), p. 31.
    ${ }^{6}$ D. Chwolsohn, Die Ssabier und Ssabismus, vol. 2, Amsterdam 1965, p. 22.

[^3]:    ' Abū'l-Rayhañ al-Bîrûnî, The Book of Instruction in the Elements of the Art of Astrology, ed. and transl. by R.R. Wright, London, Luzac, 1934.
    ${ }^{8}$ G .B. Tibbets, Arab Navigation in the Indian Ocean Before the Coming of Fortuguese: Iranslation of Kitāb al-Fawāid fi Usūl al-Bahr wa'l-Qawā̄id by Ahmad ibn Mājid all-Najeli, London, Royal Asiatic Society, 1981, p. 159.
    ${ }^{\text {y }}$ F. K. Ginzel, Handbuch der mathematischen und technischen Chronologie, Vol. 1-3 LeipzigBerlin, Teubner, 1906-1914.

    10 B. A. Rosenfeld, "The Planets and the Days of the Weck", Istoriko-Astronomicheskie Issledovaniya, vol. 22, Moscow: Nauka, pp. 367-380, 1990 (Russian).

